The Thermodynamics of Linear Fluids and Fluid Mixtures by Pekař & Samohýl

## Page 182, equation (4.178)

The dissipation  $\Pi_0$  defined by (4.171) can be written as follows:

$$\Pi_0 = -\sum_{\beta=1}^{n-1} \left( g_\beta - g_n \right) r_\beta = -\sum_{\beta=1}^{n-1} g_\beta r_\beta + g_n \sum_{\beta=1}^{n-1} r_\beta.$$
(1)

From balance (4.20) follows:

$$r_n = -\sum_{\beta=1}^{n-1} r_\beta \tag{2}$$

Using (2) in (1) we have:

$$\Pi_{0} = -\sum_{\beta=1}^{n-1} g_{\beta} r_{\beta} - g_{n} r_{n} = -\sum_{\alpha=1}^{n} g_{\alpha} r_{\alpha}.$$
(3)

Substituting from (4.172) and (4.26) into (3) successively we get:

$$-\sum_{\alpha=1}^{n} g_{\alpha} r_{\alpha} = -\sum_{\alpha=1}^{n} \frac{\mu_{\alpha}}{M_{\alpha}} r_{\alpha} = -\sum_{\alpha=1}^{n} \mu_{\alpha} J^{\alpha}.$$
 (4)

Referring to eqs. (4.173) and (4.33) the last product in (4) can be written:

$$-\sum_{\alpha=1}^{n}\mu_{\alpha}J^{\alpha} = -\vec{\mu}.\vec{J}.$$
(5)

Introducing the decomposition of the chemical potential, (4.174), we obtain:

$$-\vec{\mu}.\vec{J} = -(-\vec{A} + \vec{B}).\vec{J} = \vec{A}.\vec{J}$$
(6)

where we used the facts that  $\vec{B} \in \mathcal{W}$  ((4.174)),  $\vec{J} \in \mathcal{V}$  ((4.36)), and  $\mathcal{W} \perp \mathcal{V}$  (after (4.36) and also (4.174)) from which  $\vec{B}.\vec{J} = 0$  follows.

The last product in (6) can be written with the help of (4.43) and (4.175) as follows:

$$\vec{A}.\vec{J} = \sum_{p=1}^{n-h} J_p A^p \tag{7}$$

Combining (4.171) with (3)-(7), eq.(4.178) results.

Note that the whole procedure can be generalized to a mixture of reacting and non-reacting components. Without loss of generality let us suppose that the first *m* components are reacting and components m + 1, m + 2, ..., n are non-reacting. Then  $\Pi_0 = -\sum_{\psi=1}^{m-1} (g_{\psi} - g_m) r_{\psi}$ ,  $\sum_{\varphi=m+1}^n g_{\varphi} r_{\varphi} = 0$  can be used in balance (4.20) and instead of (2) we have  $r_m = -\sum_{\psi=1}^{m-1} r_{\psi}$ ; the other parts of the derivation remain unchanged as well as the final result (4.178).